

8.5.1

$$r = 3 \sec \theta$$

$$r = \frac{3}{\cos \theta}$$

$$r \cdot \cos \theta = 3$$

$$x = 3$$

Loddrett linje gjennom $x=3$

8.5.2

$$r = -2 \csc \theta$$

$$r = -\frac{2}{\sin \theta}$$

$$r \cdot \sin \theta = -2$$

$$y = -2$$

Horisontal linje gjennom $y=-2$

8.5.3

$$r = \frac{5}{3 \sin \theta - 4 \cos \theta}$$

$$3r \sin \theta - 4r \cos \theta = 5$$

$$3y - 4x = 5$$

$$3y = 4x + 5$$

$$y = \frac{4}{3}x + \frac{5}{3}$$

Ret linje med stigningstall

$\frac{4}{3}$ og konstantledd $\frac{5}{3}$

8.5.4

$$r = \sin \theta + \cos \theta$$

$$r^2 = r \sin \theta + r \cos \theta$$

$$x^2 + y^2 = y + x$$

$$x^2 - x + y^2 - y = 0$$

$$\left(x + \frac{-1}{2}\right)^2 - \frac{(-1)^2}{4} + \left(y + \frac{-1}{2}\right)^2 - \frac{(-1)^2}{4} = 0$$

$$\left(x - \frac{1}{2}\right)^2 + \left(y - \frac{1}{2}\right)^2 = \left(\frac{\sqrt{1}}{2}\right)^2$$

Sirkel med senter i $(\frac{1}{2}, \frac{1}{2})$ og radius $\sqrt{\frac{1}{2}}$.

(8.5.5)

$$r^2 = \csc 2\theta$$

$$r^2 = \frac{1}{\sin 2\theta} = \frac{1}{2 \sin \theta \cdot \cos \theta}$$

$$r \cdot \sin \theta \cdot r \cdot \cos \theta = \frac{1}{2}$$

$$x \cdot y = \frac{1}{2}$$

$$y = \frac{1}{2x}$$

Hyperbel

8.5.6

$$r = \sec \theta \cdot \tan \theta$$

$$r = \frac{1}{\cos \theta} \cdot \frac{\sin \theta}{\cos \theta}$$

$$r^2 \cdot \cos^2 \theta = r \cdot \sin \theta$$

$$x^2 = y$$

parabel

8.5.7

$$r = \sec \theta (1 + \tan \theta)$$

$$r = \frac{1}{\cos \theta} \left(1 + \frac{\sin \theta}{\cos \theta} \right)$$

$$r \cos \theta = 1 + \frac{\sin \theta}{\cos \theta}$$

$$r \cos^2 \theta = \cos \theta + \sin \theta$$

$$r^2 \cos^2 \theta = r \cos \theta + r \sin \theta$$

$$x^2 = x + y$$

$$y = x^2 - x$$

parabel

8.5.8

$$r = \frac{2}{\sqrt{\cos^2 \theta + 4 \sin^2 \theta}}$$

$$r^2 \cos^2 \theta + 4r^2 \sin^2 \theta = 4$$

$$x^2 + 4y^2 = 4$$

$$\frac{x^2}{2^2} + \frac{y^2}{1^2} = 1$$

Ellipse

8.5.9

$$r = \frac{1}{1 - \cos \theta}$$

$$r - r \cos \theta = 1$$

$$r - x = 1$$

$$r = x + 1$$

$$r^2 = (x + 1)^2$$

$$x^2 + y^2 = (x + 1)^2$$

$$x^2 + y^2 = x^2 + 2x + 1$$

$$y^2 = 2x + 1$$

$$x = \frac{1}{2}y^2 - \frac{1}{2}$$

parabel

8.5.10

$$r = \frac{2}{2 - \cos \theta}$$

$$2r - r \cos \theta = 2$$

$$2r - x = 2$$

$$2r = x + 2$$

$$4r^2 = (x + 2)^2$$

$$4(x^2 + y^2) = x^2 + 4x + 4$$

$$4x^2 - x^2 + -4x + 4y^2 - 4 = 0$$

$$3x^2 - 4x + 4y^2 - 4 = 0$$

$$3\left(x + \frac{-4}{2 \cdot 3}\right)^2 - \frac{(-4)^2}{4 \cdot 3} + 4y^2 - 4 = 0$$

$$3\left(x - \frac{2}{3}\right)^2 + 4y^2 = \frac{16}{3}$$

$$\frac{\left(x - \frac{2}{3}\right)^2}{\left(\frac{4}{3}\right)^2} + \frac{y^2}{\left(\frac{2}{\sqrt{3}}\right)^2} = 1$$

Ellipse

8.5.11

$$r = \frac{2}{1-2\sin\theta}$$

$$r - 2r\sin\theta = 2$$

$$r - 2y = 2$$

$$r = 2 + 2y = 2(y+1)$$

$$r^2 = 4(y+1)^2$$

$$x^2 + y^2 = 4(y^2 + 2y + 1)$$

$$x^2 + y^2 - 4y^2 - 8y - 4 = 0$$

$$x^2 - 3y^2 - 8y - 4 = 0$$

$$x^2 - 3\left(y + \frac{-8}{2 \cdot (-3)}\right)^2 - \frac{(-8)^2}{4 \cdot (-3)} - 4 = 0$$

$$x^2 - 3\left(y + \frac{4}{3}\right)^2 = -\frac{4}{3}$$

$$\frac{\left(y + \frac{4}{3}\right)^2}{\left(\frac{2}{3}\right)^2} - \frac{x^2}{\left(\frac{2}{\sqrt{3}}\right)^2} = 1$$

Hyperbel

8.5.12

$$r = \frac{2}{1+\sin\theta}$$

$$r + r\sin\theta = 2$$

$$r^2 = (2-y)^2$$

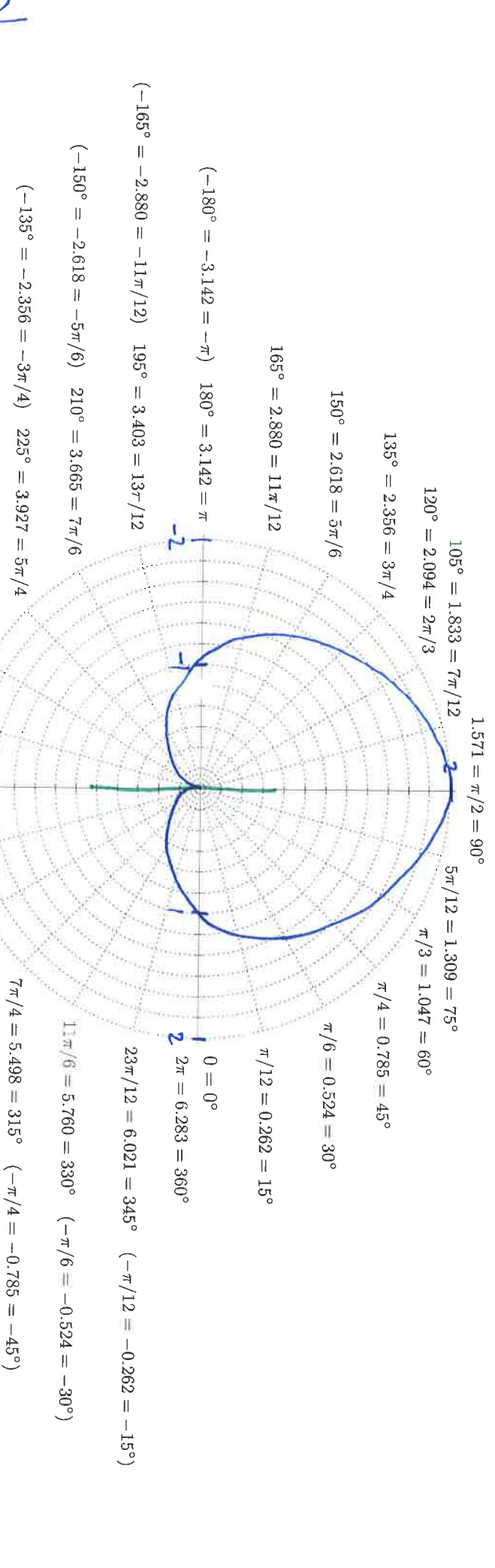
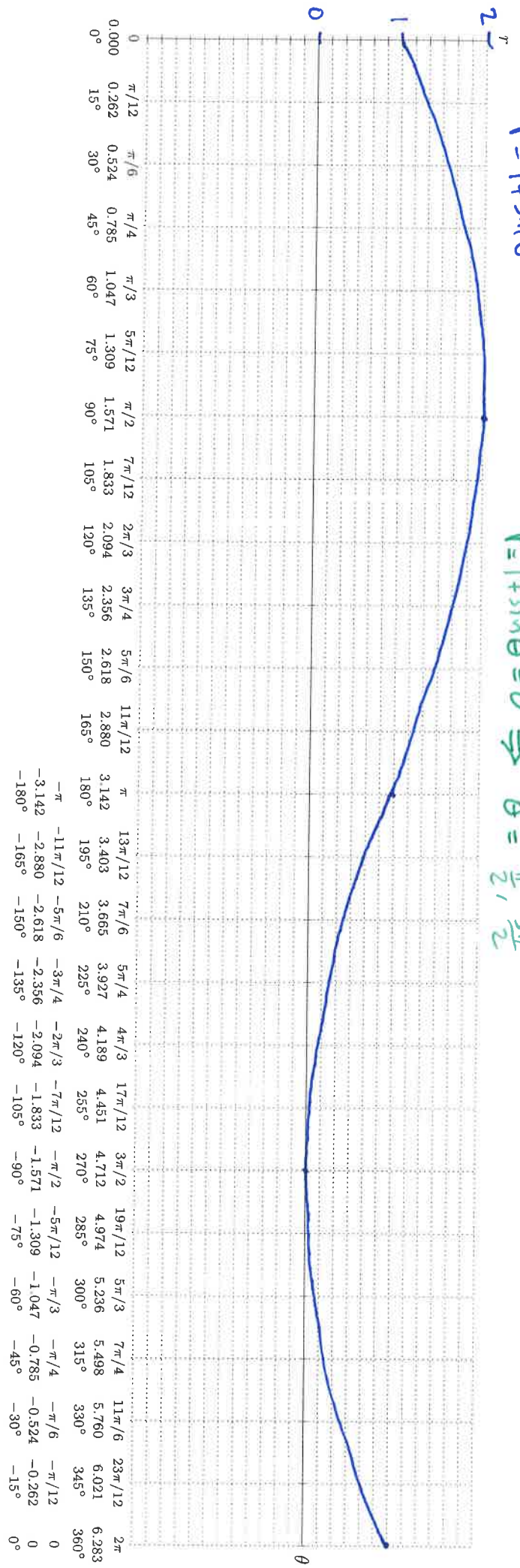
$$x^2 + y^2 = 4 - 4y + y^2$$

$$x^2 = 4 - 4y$$

parabel

$$r = 1 + \sin \theta$$

$$r = 1 + \sin \theta = 0 \Rightarrow \theta = \frac{\pi}{2}, \frac{3\pi}{2}$$

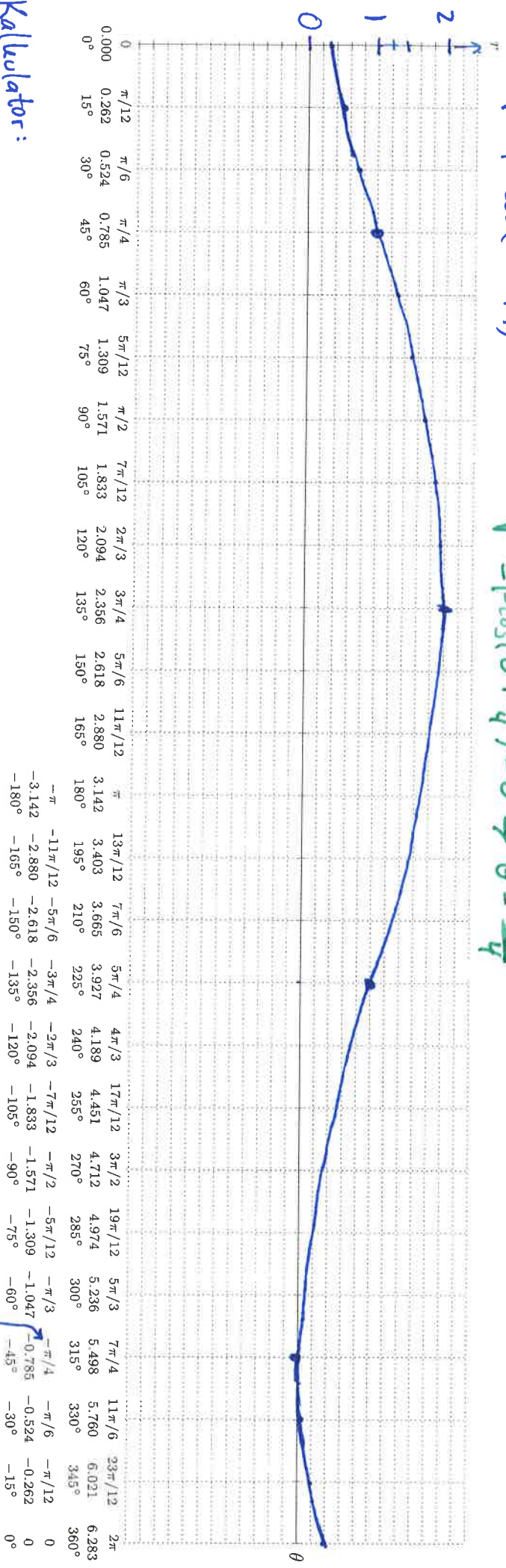


- $150^\circ = 2.618 = 5\pi/6$
- $135^\circ = 2.356 = 3\pi/4$
- $120^\circ = 2.094 = 2\pi/3$
- $105^\circ = 1.833 = 7\pi/12$
- $90^\circ = 1.571 = \pi/2$
- $75^\circ = 1.309 = 5\pi/12$
- $60^\circ = 1.047 = \pi/3$
- $45^\circ = 0.785 = \pi/4$
- $30^\circ = 0.524 = \pi/6$
- $15^\circ = 0.262 = \pi/12$
- $0 = 0^\circ$
- $2\pi = 6.283 = 360^\circ$
- $23\pi/12 = 6.021 = 345^\circ$
- $11\pi/6 = 5.760 = 330^\circ$
- $7\pi/4 = 5.498 = 315^\circ$
- $5\pi/3 = 5.236 = 300^\circ$
- $19\pi/12 = 4.974 = 285^\circ$
- $3\pi/2 = 4.712 = 270^\circ$
- $5\pi/4 = 4.451 = 225^\circ$
- $4\pi/3 = 4.189 = 240^\circ$
- $17\pi/12 = 4.451 = 17\pi/12$
- $3\pi/2 = 4.712 = 270^\circ$
- $5\pi/3 = 5.236 = 300^\circ$
- $7\pi/4 = 5.498 = 315^\circ$
- $11\pi/6 = 5.760 = 330^\circ$
- $13\pi/12 = 3.403 = 13\pi/12$
- $180^\circ = 3.142 = \pi$
- $150^\circ = 2.880 = 11\pi/12$
- $180^\circ = -\pi$
- $195^\circ = 3.403 = 13\pi/12$
- $210^\circ = 3.665 = 7\pi/6$
- $225^\circ = 3.927 = 5\pi/4$
- $240^\circ = 4.189 = 4\pi/3$
- $255^\circ = 4.451 = 17\pi/12$
- $270^\circ = 4.712 = 3\pi/2$
- $285^\circ = 4.974 = 5\pi/3$
- $300^\circ = 5.236 = 5\pi/3$
- $315^\circ = 5.498 = 7\pi/4$
- $330^\circ = 5.760 = 11\pi/6$
- $345^\circ = 6.021 = 23\pi/12$
- $360^\circ = 6.283 = 2\pi$
- $(-165^\circ = -2.880 = -11\pi/12)$
- $(-150^\circ = -2.618 = -5\pi/6)$
- $(-135^\circ = -2.356 = -3\pi/4)$
- $(-120^\circ = -2.094 = -2\pi/3)$
- $(-105^\circ = -1.833 = -7\pi/12)$
- $(-90^\circ = -1.571 = -\pi/2)$
- $(-75^\circ = -1.309 = -5\pi/12)$
- $(-60^\circ = -1.047 = -\pi/3)$
- $(-45^\circ = -0.785 = -\pi/4)$
- $(-30^\circ = -0.524 = -\pi/6)$
- $(-15^\circ = -0.262 = -\pi/12)$

8.5.13

$$r = 1 - \cos(\theta + \pi/4)$$

$$r = 1 - \cos(\theta + \pi/4) = 0 \Rightarrow \theta = \frac{7\pi}{4}$$



Kalkulator:

Lager tabell med

steglengde $\frac{\pi}{12} = 0.261799$

$$105^\circ = 1.833 = 7\pi/12$$

$$120^\circ = 2.094 = 2\pi/3$$

$$135^\circ = 2.356 = 3\pi/4$$

$$150^\circ = 2.618 = 5\pi/6$$

$$165^\circ = 2.880 = 11\pi/12$$

$$(-180^\circ = -3.142 = -\pi) \quad 180^\circ = 3.142 = \pi$$

$$(-165^\circ = -2.880 = -11\pi/12) \quad 195^\circ = 3.403 = 13\pi/12$$

$$(-150^\circ = -2.618 = -5\pi/6) \quad 210^\circ = 3.665 = 7\pi/6$$

$$(-135^\circ = -2.356 = -3\pi/4) \quad 225^\circ = 3.927 = 5\pi/4$$

$$(-120^\circ = -2.094 = -2\pi/3) \quad 240^\circ = 4.189 = 4\pi/3$$

$$(-105^\circ = -1.833 = -7\pi/12) \quad 255^\circ = 4.451 = 17\pi/12$$

$$4.712 = 3\pi/2 = 270^\circ$$

$$(-1.571 = -\pi/2 = -90^\circ)$$

$$1.571 = \pi/2 = 90^\circ$$

$$105^\circ = 1.833 = 7\pi/12$$

$$120^\circ = 2.094 = 2\pi/3$$

$$135^\circ = 2.356 = 3\pi/4$$

$$150^\circ = 2.618 = 5\pi/6$$

$$165^\circ = 2.880 = 11\pi/12$$

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$$(-120^\circ = -2.094 = -2\pi/3) \quad 240^\circ = 4.189 = 4\pi/3$$

$$(-105^\circ = -1.833 = -7\pi/12) \quad 255^\circ = 4.451 = 17\pi/12$$

$$4.712 = 3\pi/2 = 270^\circ$$

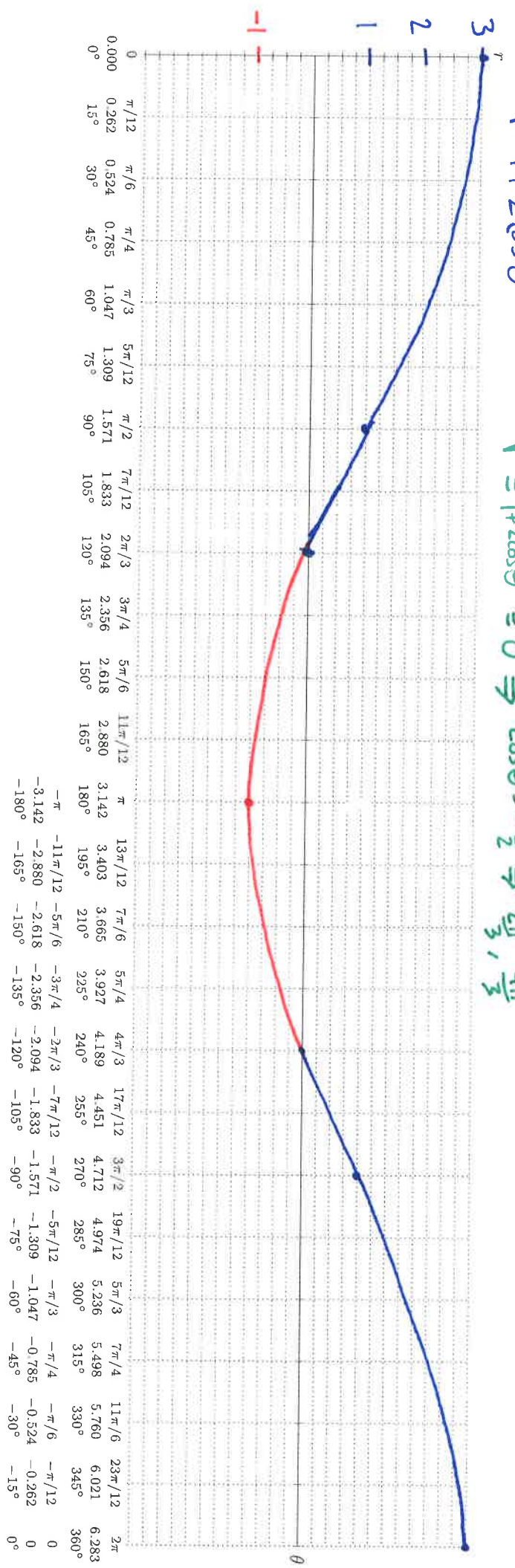
$$(-1.571 = -\pi/2 = -90^\circ)$$

$$\cos(\theta + \pi/4) = 1 \text{ n\u00e5r } \theta = -\frac{7\pi}{4}$$

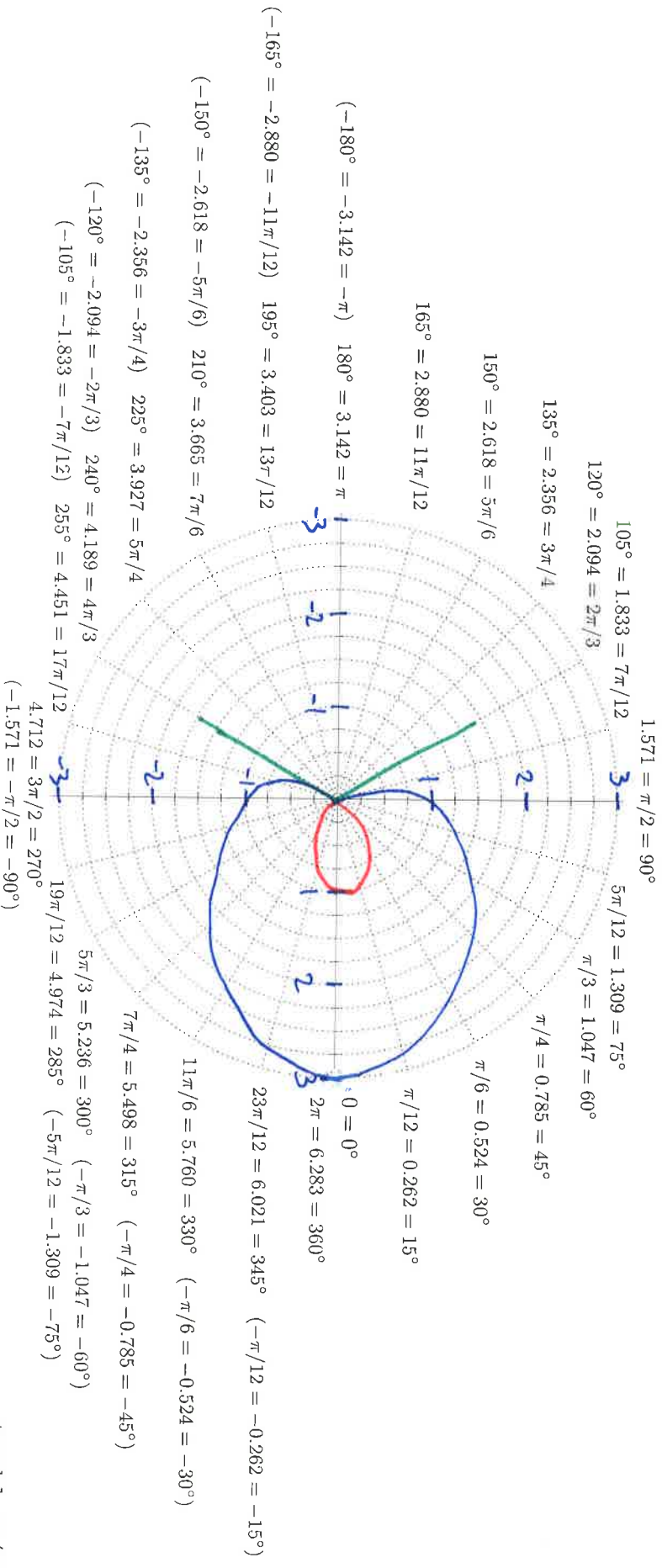
8.5.14

$$r = 1 + 2\cos\theta$$

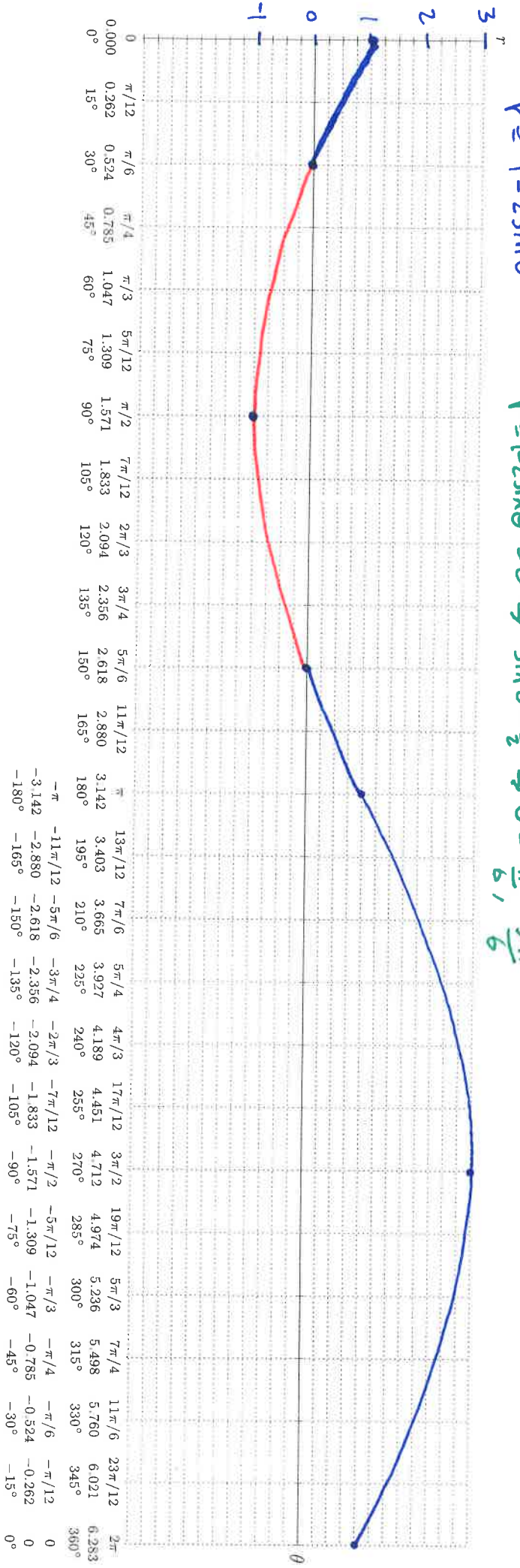
$$r = 1 + 2\cos\theta = 0 \Rightarrow \cos\theta = -\frac{1}{2} \Rightarrow \frac{2\pi}{3}, \frac{4\pi}{3}$$



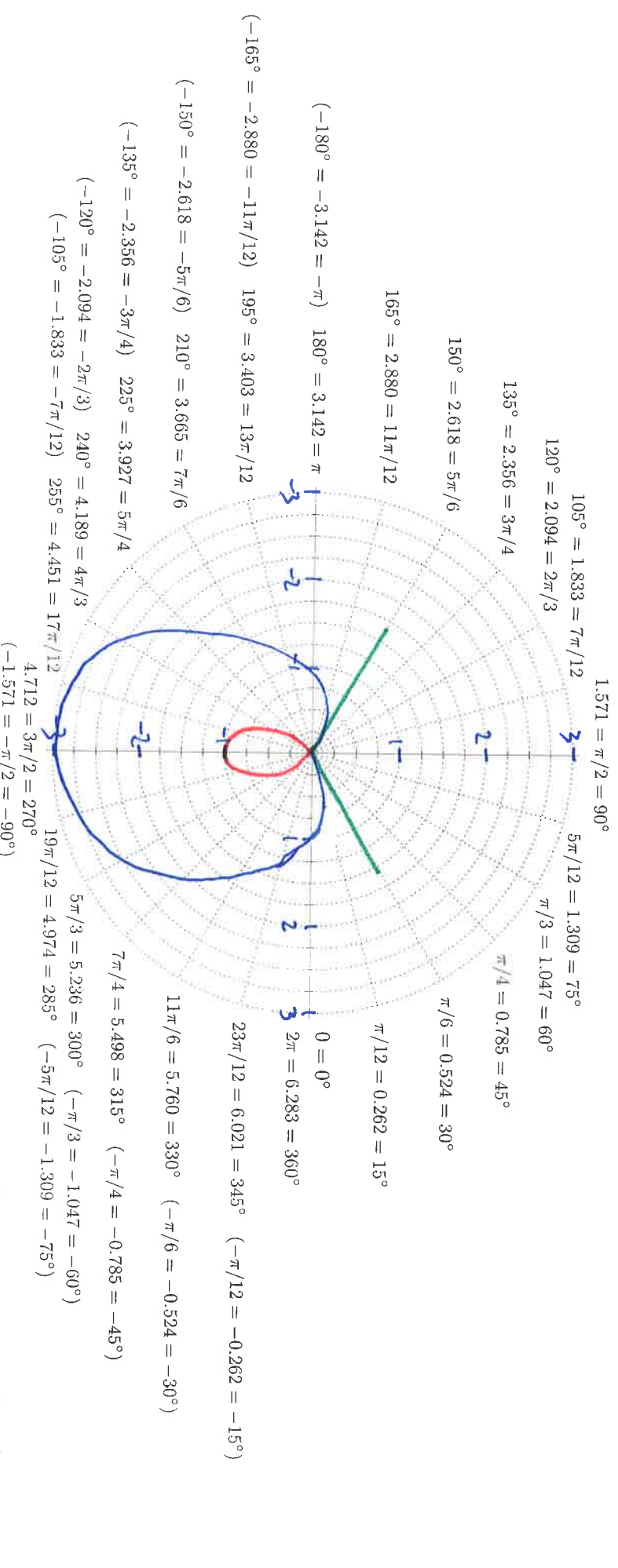
8.5.15



$r = 1 - 2\sin\theta$
 $r = 1 - 2\sin\theta = 0 \Rightarrow \sin\theta = \frac{1}{2} \Rightarrow \theta = \frac{\pi}{6}, \frac{5\pi}{6}$

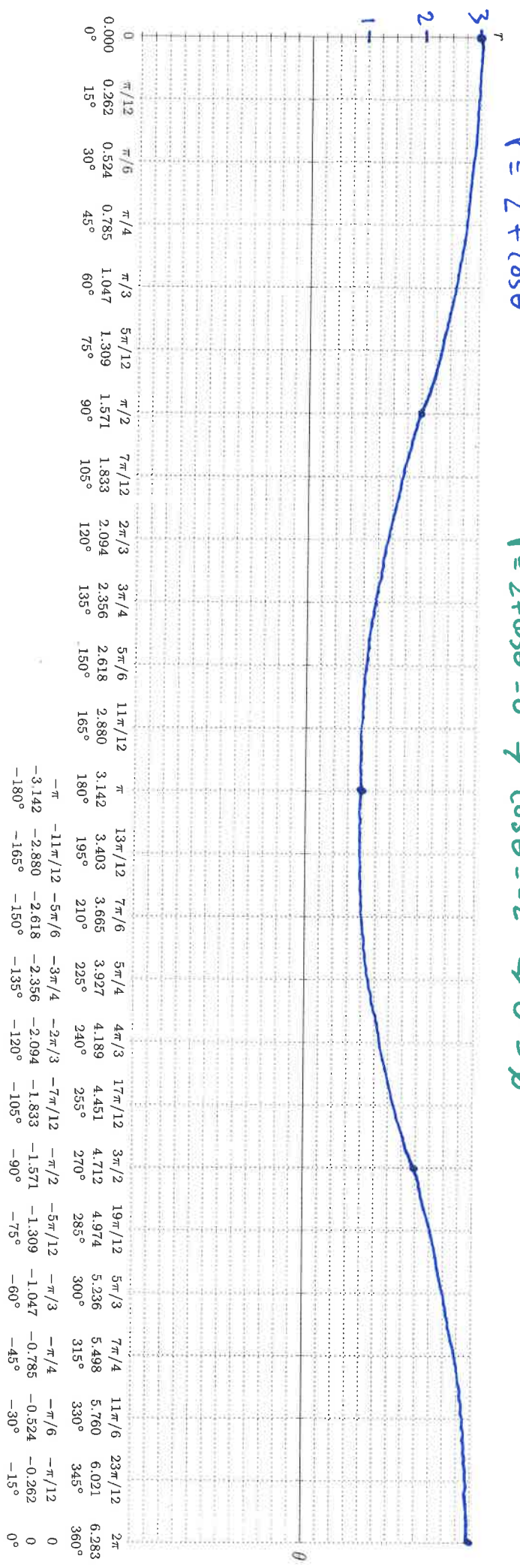


8.5.16

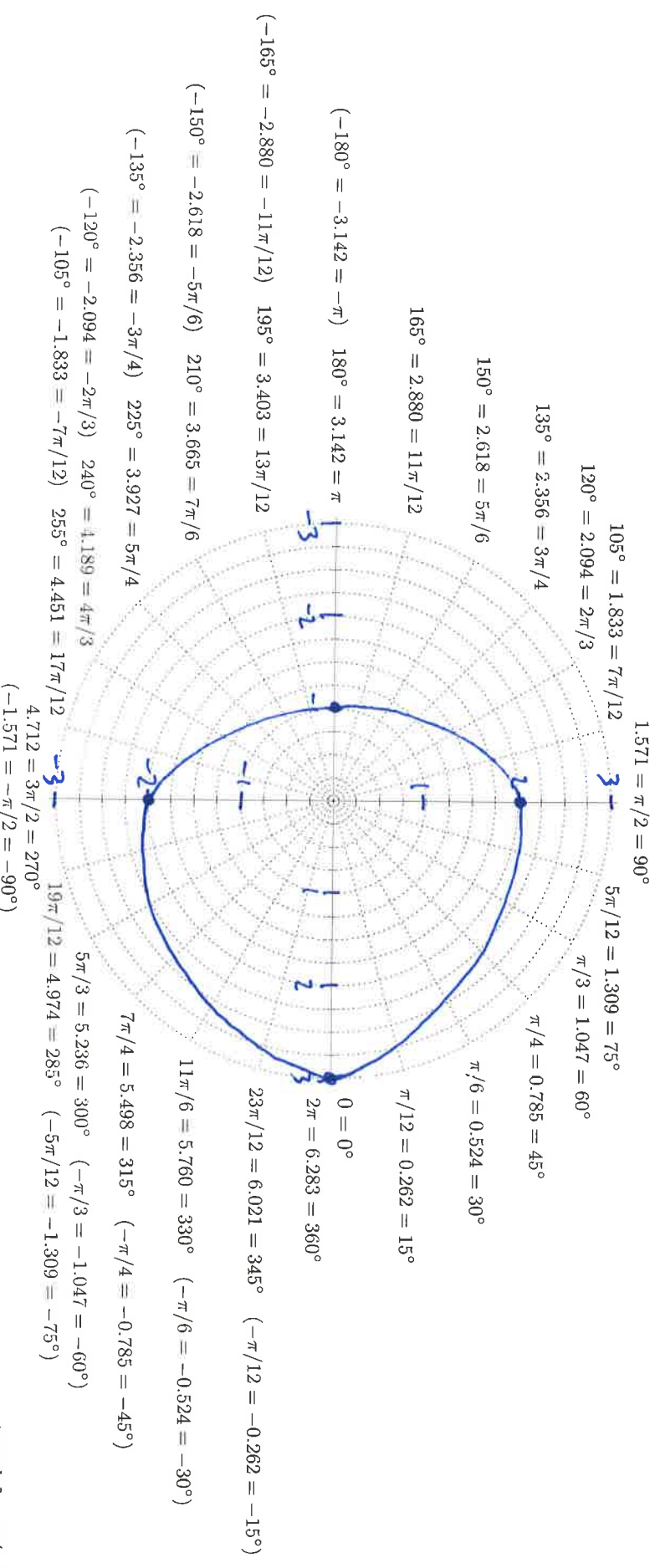


$$r = 2 + \cos \theta$$

$$r = 2 + \cos \theta = 0 \Rightarrow \cos \theta = -2 \Rightarrow \theta = \emptyset$$

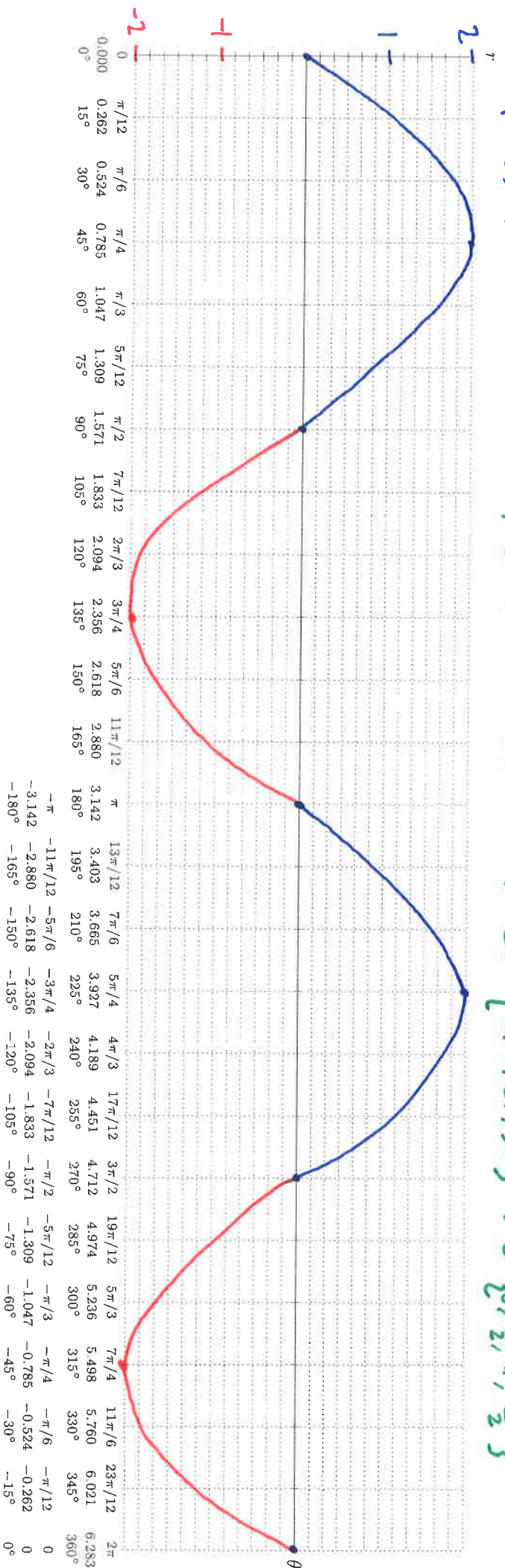


8.5.17

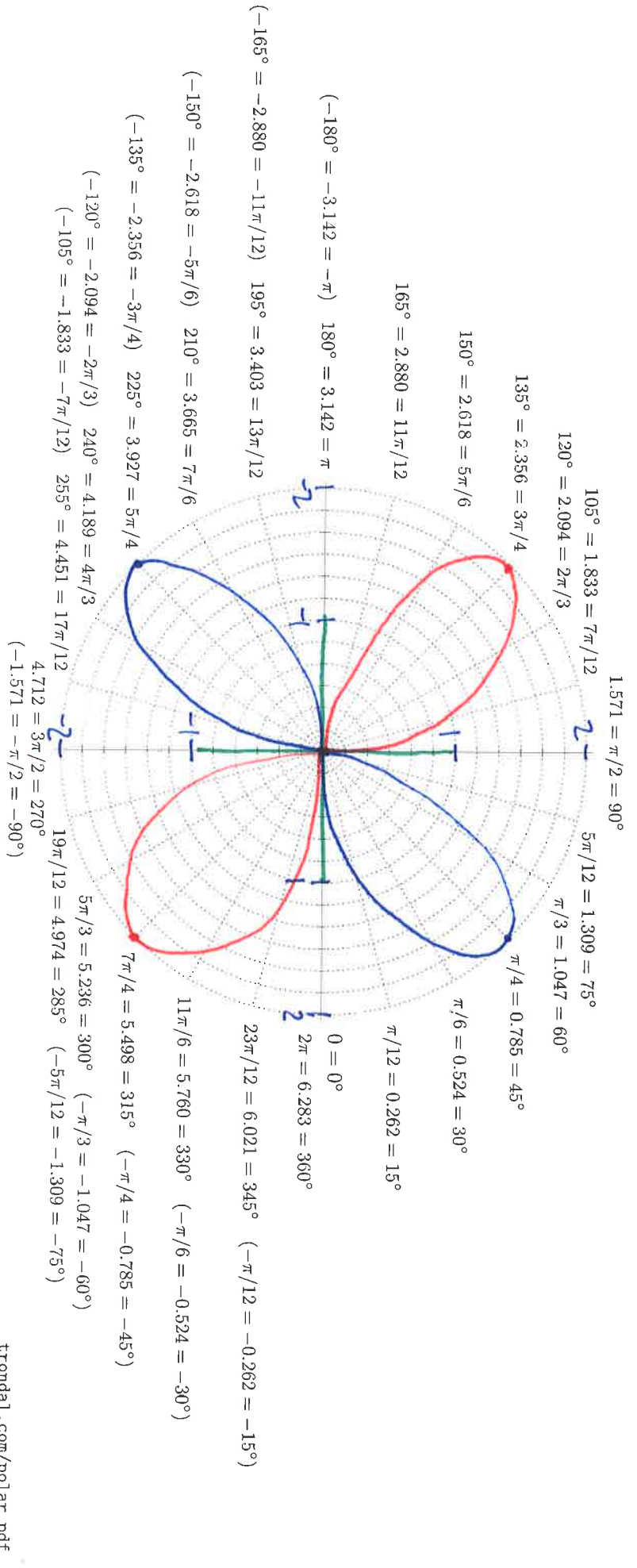


$$r = 2 \sin 2\theta$$

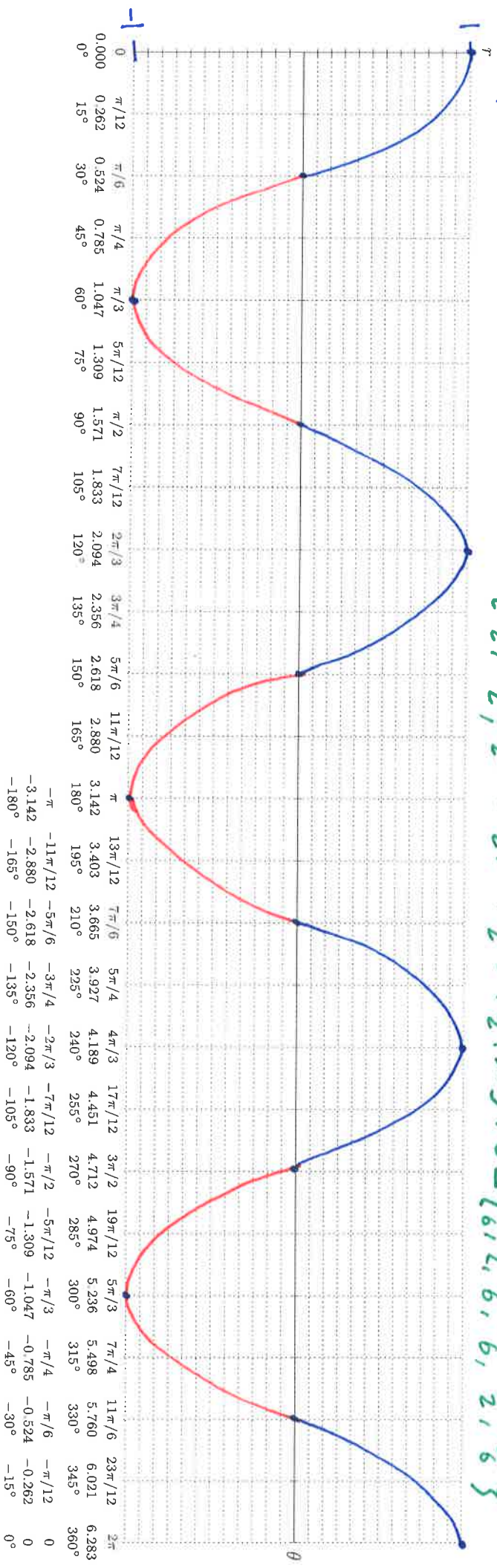
$$r = 2 \sin 2\theta = 0 \Rightarrow \sin 2\theta = 0 \Rightarrow 2\theta = \{0, \pi, 2\pi, 3\pi\} \Rightarrow \theta = \{0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}\}$$



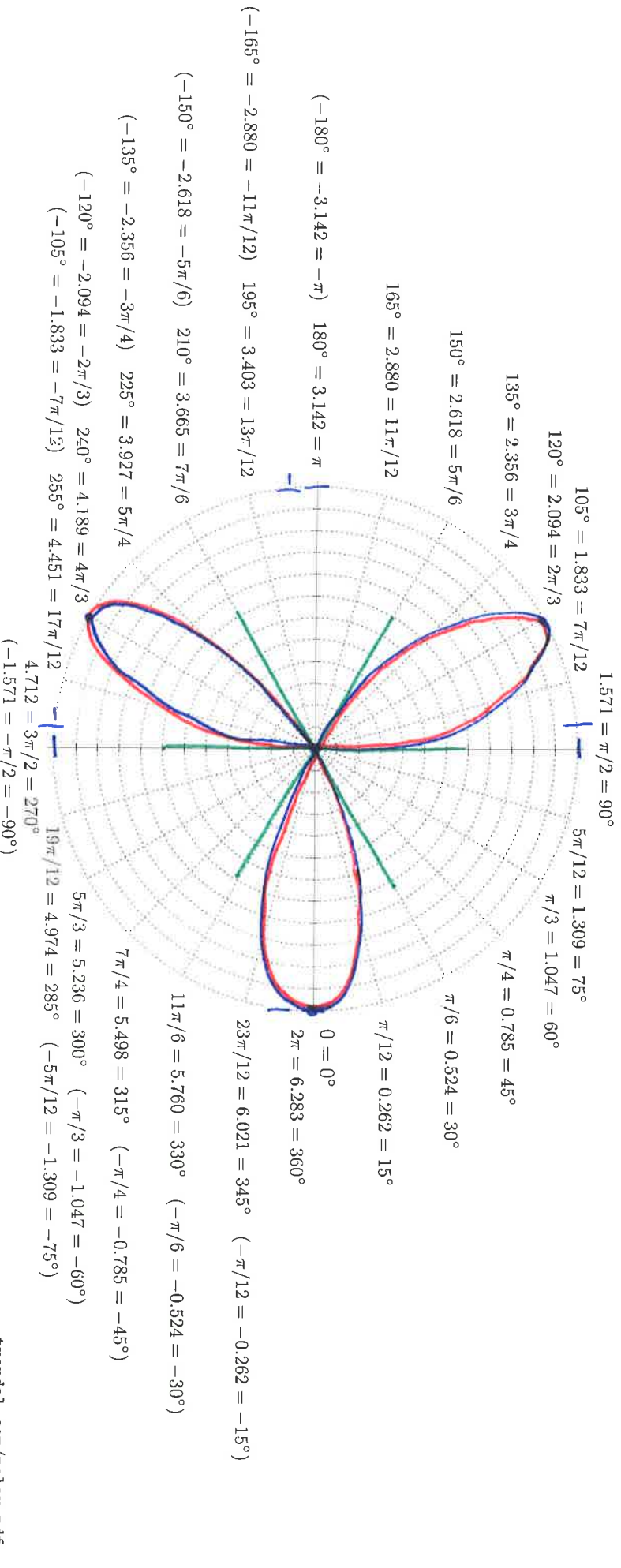
8.5.18



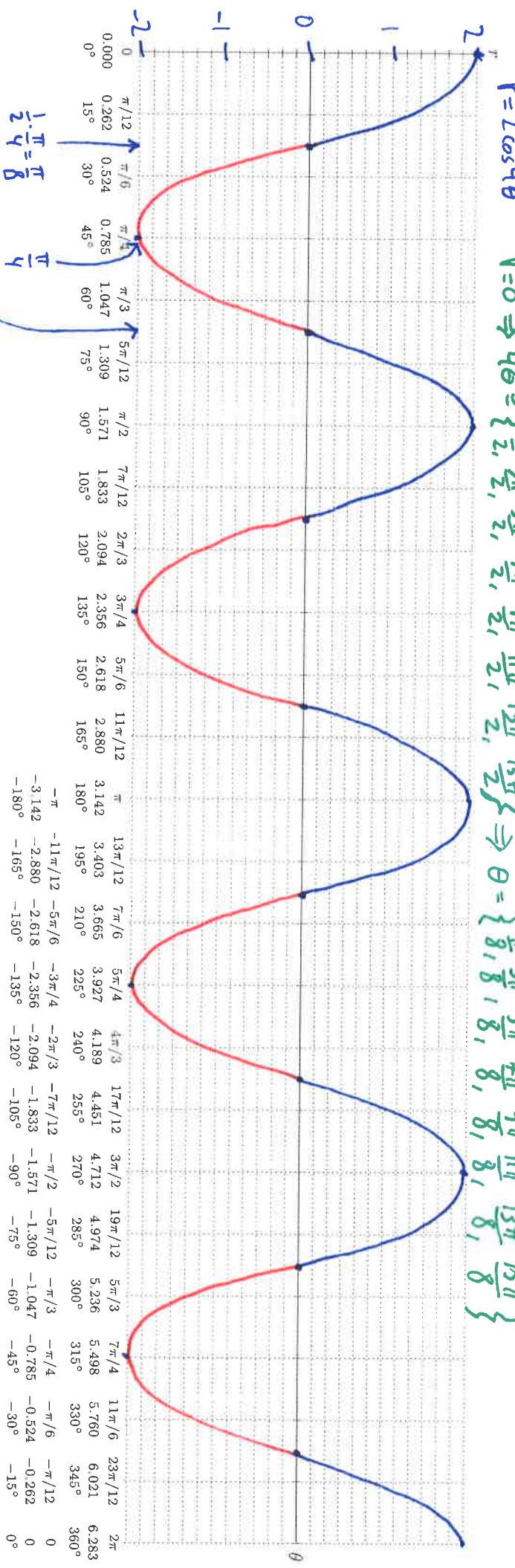
$r = \cos 3\theta \Rightarrow 3\theta = \left\{ \frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{2} + 2\pi, \frac{3\pi}{2} + 2\pi, \frac{\pi}{2} + 3\pi, \frac{3\pi}{2} + 3\pi \right\} \Rightarrow \theta = \left\{ \frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}, \frac{3\pi}{2}, \frac{7\pi}{6}, \frac{11\pi}{6} \right\}$



8.5.19



$r = 2 \cos 4\theta$ $r = 0 \Rightarrow 4\theta = \left\{ \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}, \frac{9\pi}{2}, \frac{11\pi}{2}, \frac{13\pi}{2}, \frac{15\pi}{2} \right\} \Rightarrow \theta = \left\{ \frac{\pi}{8}, \frac{3\pi}{8}, \frac{5\pi}{8}, \frac{7\pi}{8}, \frac{9\pi}{8}, \frac{11\pi}{8}, \frac{13\pi}{8}, \frac{15\pi}{8} \right\}$



$\frac{1}{2} \left(\frac{\pi}{3} + \frac{5\pi}{12} \right) = \frac{3\pi}{8}$

8.5.20

